

2018

## Pulsar selection using fuzzy knn classifier

Taha M. Mohamed

*Faculty of Computers and Information, Helwan University, Egypt, tahamahdy3000@yahoo.com*

Follow this and additional works at: <https://digitalcommons.aaru.edu.jo/fcij>



Part of the [Computer Engineering Commons](#)

---

### Recommended Citation

Mohamed, Taha M. (2018) "Pulsar selection using fuzzy knn classifier," *Future Computing and Informatics Journal*: Vol. 3 : Iss. 1 , Article 1.

Available at: <https://digitalcommons.aaru.edu.jo/fcij/vol3/iss1/1>

This Article is brought to you for free and open access by Arab Journals Platform. It has been accepted for inclusion in Future Computing and Informatics Journal by an authorized editor. The journal is hosted on [Digital Commons](#), an Elsevier platform. For more information, please contact [rakan@aarj.edu.jo](mailto:rakan@aarj.edu.jo), [marah@aarj.edu.jo](mailto:marah@aarj.edu.jo), [dr\\_ahmad@aarj.edu.jo](mailto:dr_ahmad@aarj.edu.jo).

# Pulsar selection using fuzzy *knn* classifier

Taha M. Mohamed\*

Faculty of Computers and Information, Helwan University, Egypt

Received 13 November 2017; accepted 21 November 2017

Available online 21 December 2017

## Abstract

Pulsars are rare type of stars that emit radio signals that could be detected from earth. Astronomy scientists give more attention to this type of stars for many reasons. In the near past, the problem of pulsar selection was carried out manually. Recently, neural network techniques are proposed to solve the problem. In this paper, we present a novel technique to efficiently selecting pulsars. The proposed algorithm is based on the fuzzy knn classifier. Results show that, the proposed algorithm outperforms five other classifiers, including neural network classifiers, using three evaluation metrics. The proposed algorithm is evaluated on the recent HITRU 2 dataset.

Copyright © 2017 Faculty of Computers and Information Technology, Future University in Egypt. Production and hosting by Elsevier B.V. This is an open access article under the CC BY-NC-ND license (<http://creativecommons.org/licenses/by-nc-nd/4.0/>).

**Keywords:** Fuzzy classifiers; Fuzzy knn; HITRU 2; Pulsar selection

## 1. Introduction

Pulsars are a rare type of stars that produce radio signals detectable from the Earth. When pulsars rotate, their emission beam sweeps across the sky. So, a detectable pattern of broadband radio emission is produced when this beam crosses our line of sight. The pattern repeats periodically when pulsars rotate rapidly [1,7]. Pulsars are laboratories for extreme physics unachievable on the earth [5]. They are very important as they may be used as probes of space-time, inter stellar medium, super fluid, states of matter, and many others [1,5,7]. Currently, there are around 2200 known pulsars in the Milky Way, the Magellanic clouds, and globular clusters [5].

However, searching for pulsars is not a simple task. Discovering pulsars involves identifying periodic signals in observational data. Then, these data is reduced to a set of diagnostic values and graphical representations called a candidate [2]. Unfortunately, most of the candidates are

caused by radio frequency interference (RFI) and noise, that incorrectly look like pulsars [1,7].

Pulsar surveys are carried out by pointing the telescope at a region of the sky for several minutes to hours. The observational data is then recorded, and the telescope is moving to another region of the sky looking for new pulsars [3]. The pulsar candidates are the recorded plots and statistics of radio signals that is the raw material for further analysis. The candidates should be further inspected by either automatically, or by human expert, to determine their authenticity [1]. Until recently, the selection of promising candidates to be observed again for confirmation is heavily dependent on human inspection. However, the human inspection is a subjective, time-consuming, and error prone process [1,2]. Moreover, those of likely pulsars are highlighted for further analysis, and possibly allocated extra telescope time for confirmation. The candidate ‘selection’ process is the process of deciding which a candidate is really a pulsar or not [1]. Until recently [1], the candidate selection process was a manual task. However, the manual selection is impractical due to the large amount of candidates produced by recent high technology telescopes [1]. Recently, the research is oriented to machine learning approaches to solve the candidates selection problem.

\* Corresponding author

E-mail address: [tahamahdy3000@yahoo.com](mailto:tahamahdy3000@yahoo.com).

Peer review under responsibility of Faculty of Computers and Information Technology, Future University in Egypt.

The recent High Time Resolution Universe (HTRU) survey is a sky survey conducted in 2008, and has been recently completed. It uses the efficient *Parkes* radio telescope to search the whole visible sky for pulsars [5]. This survey produces several millions of candidates. Unfortunately, the majority of which are non pulsars that are caused either by human made radio-frequency interference (RFI), or due to noise [2,5].

Many features of the candidates are proposed in the literature [1]. Among them, the features proposed by Ref. [1] that experimentally prove superiority over other used features. These features are tested on HITRU1 [2], HITUE2 [1], and LOTAAS [1] datasets. The authors in Ref. [1] claims that, the features maximize the separation between noise and non-noise candidates. Another advantage of these proposed features is the low number of features which avoid the curse of dimensionality problem.

The HTRU2 dataset, is the recent publicly available data set [1,8], that describes a sample of pulsar candidates collected during the High Time Resolution Universe (HTRU) Survey [1]. The data set is represented as eight variables  $X_i$   $e$   $\{X_1, \dots, X_8\}$  representing some statistical information about HTRU signals. The first four features are simple statistics obtained from the integrated pulse profile. The remaining four features are similarly obtained from the DM-SNR curve [1]. The goal of the classification process is to classify the given candidates as pulsars or non pulsars. The binary labels, the class label,  $Y = \{0, 1\}$ , where  $Y = 0$  refers to non-pulsar. On the contrary, when  $Y = 1$ , this refers to existing of pulsars.

Among the various machine learning approaches, the fuzzy  $K$ -nearest Neighbors ( $knn$ ) classifier, which is one of the most known and effective methods in supervised classification [10]. To the best of our knowledge, no research is conducted to evaluate fuzzy classifiers in pulsar selection problems. However, neural networks are the dominant machine learning techniques used in this domain.

In this paper, a new fuzzy  $knn$  classifier is proposed to solve the pulsar selection problem. The proposed algorithm is tested on the publicly available HITRU2 data set [8], and proves superiority over other classifiers used in the literature. The rest of this paper is organized as follows; Section 2 presents the necessary background. Section 3 presents the related work. Section 4 presents the proposed algorithm. The experimental results are described in Section 5. Finally, the paper is concluded in Section 6.

## 2. Background

Neural networks, and perceptron techniques, are good classifiers in case of classes that are separable. However, this is not always the case, in most situations, some of the samples of the given classes are ambiguous and seem to belong to more than one class. The neural networks converge if there is a separable plane between classes. If this is not the case, the neural network may not converge. In this case, there are some fuzziness of the membership of a test pattern to more than one class. The fuzzy classifiers are more useful in this case, and also perform better.

Additionally, the Bayesian classifiers guarantee the optimal error rate in classification in case of previously knowing the prior probabilities and class densities. The available sample size should be large enough for perfect classification. However, if one of the previous conditions is violated, the  $k$  nearest neighbor ( $knn$ ) classifier, and also the fuzzy  $knn$ , classifiers present better alternative to the Bayesian classifiers, and also perform more better. Another advantage of using  $knn$  and fuzzy  $knn$  is the simplicity and the economical computational requirements.

The nearest neighbor classifier is a non parametric classification algorithm. The problem addressed by the nearest neighbor classifier ( $NN$ ) is the assignment of unknown test pattern  $x$  to one of the given classes  $C_i$ . The solution given by the  $NN$  classifier is the minimum distance that could be computed using the Euclidean distance or any other distance. For example, the Euclidean distance is given by equation (1) as:

$$d = \sqrt{\sum_{j=1}^n (|C_i(j) - x|)^2} \quad (1)$$

where  $n$  is the feature vector size. Next, the unknown pattern  $x$  is assigned to the class with minimum distance. It is shown that, the error rate of the  $NN$  classifier is bounded by no more than twice the error rate obtained by Bayesian classifier. Additionally, in the  $knn$  classifier, as  $k$  increases, the error rate decreases asymptotically. There are some problems with the  $NN$  classifier. The most important problem is the equal distance problem between the test pattern and more than one class. This problem is partially solved using the  $knn$  classifier. In this classifier, the  $k$  nearest neighbors are computed. The test pattern is classified as belonging to the class with the maximum number of neighbors. However,  $NN$ , and  $knn$ , algorithms are still suffering from some other problems. The most important problem is that, they treat all samples with equal importance. However, this is not always the case, especially when there are some outliers in the given samples. An additional problem arises when the test pattern has an equal  $k$  to more than one class. In this case, an ambiguity occurs. Another problem is that, once a test pattern is assigned to a certain class, no indication of a class membership could be inducted [11].

The previous problems lead to the development of the fuzzy  $knn$  [11] that could give a fuzzy decision on the test pattern. The fuzzy  $knn$  assigns a membership value to a sample pattern, and then assign a membership value to each class, and assign the class label to the maximum membership value rather than assign this pattern to a particular class. The variable  $m$  determines the amount of the weights of the distances that could give larger weights to near patterns and lower weights to farther patterns. The fuzzy nearest neighbor algorithm (fuzzy  $knn$ ) is introduced in Ref. [11]. The classification results of fuzzy  $knn$  shows the superiority of this classifier over other crisp  $knn$  and other classifiers such as linear discriminant functions, Bayesian, and neural networks classifiers. An extensive survey on fuzzy  $knn$  could be found in Ref. [12].

Let  $x$  be a training set, composed of  $N$  instances  $x = \{x_0, x_1, \dots, x_N\}$  which belong to  $C$  classes [10]. Let  $Q$  be the test pattern. The fuzzy membership function of each training pattern  $U_c(x)$  is given by equation (2). Here,  $nn_c$  is the number of instances belonging to class  $c$  found among the  $k_{in}$  neighbors of  $x$ . The initial  $k$ ,  $k_{in}$ , is a constant that could take a value in the interval from 3 to 9 [10].

$$U_c(x) = \begin{cases} \left( \frac{nn_c}{k_{in}} \right) * 0.49 + 0.51, & \text{if } c = w \\ 0.49 * \left( \frac{nn_c}{k_{in}} \right), & \text{otherwise} \end{cases} \quad (2)$$

A test pattern is classified using the maximum votes that are given by equation (3).

$$V(k_j, c) = \frac{U_c(k_j) \cdot 1 / (\|Q - k_j\|)^{2/(m-1)}}{\sum_{i=1}^k (1 / (\|Q - k_i\|)^{2/(m-1)})} \quad (3)$$

where  $k_j$  is the  $j$  nearest neighbor.  $m$  is a constant often set to 2 [10,11].

### 3. Related work

Eatough et al. [4] propose the first machine learning approach in candidate selection problem. In their work, each candidate was reduced to a set of twelve numerical feature values. They used an artificial neural network to select pulsars from candidates. Bates et al. [6] describe the candidates using ten further numerical features to train neural network classifiers. Morello et al. [2] propose the SPINN system that uses the neural network by using a set of six features. In Ref. [3], the authors present the PEACE (Pulsar Evaluation Algorithm for Candidate Extraction). The authors claim that, the algorithm improves the efficiency of identifying pulsar signals [3]. Recently, in Ref. [1], the authors study the candidate filtering problem used during the past fifty years [1]. The authors propose a new method for selecting candidates using a Gaussian Hellinger Very Fast Decision Tree (GH-VFDT). They also propose a new set of features. The authors also evaluate the proposed algorithm on three pulsar candidates datasets using five different classifiers.

It is shown from the previous literature survey that, the machine learning techniques are new to the field of pulsar selection process. Until recently, the process was performed manually. However, the limitations of the manual process and the huge amount of data make the manual selection process impossible and impractical. Also, it is noted that, neural networks are the dominant classifiers used in this arena. To the maximum of our knowledge, there is no other machine learning approach that being used in solving this problem, except the modified decision tree introduced in Ref. [1].

### 4. The proposed algorithm

The proposed algorithm is a fuzzy  $knn$  algorithm proposed to solve the pulsar selection problem. The proposed algorithm

operates on HITRU2 dataset containing 8 input features  $\{X_1, \dots, X_8\}$ , and one output variable  $Y$ . The data set contains 1639 pulsar patterns and 16259 non pulsar patterns with a total of 17898 patterns. The proposed algorithm aims to enhance the accuracy, F-score, and the G-mean of the classification process. A test pattern  $x$  is used with an input samples matrix containing the sample vectors.

As, a pre processing step, the correlation matrix is constructed to discover the relationship between the input features with each other, and also the relationship between the input features and the response variable  $Y$ . Then, the membership values of each sample is computed. By using the membership function described by equation (2), all nearest neighbors are given a high membership to the class they are near from. However, the samples that are far from a class will be given a small membership value to this class.

Once the membership values are computed, the minimum distance is computed between the test pattern  $x$  and all sample vectors using equation (3). To compute the distance, the Euclidean distance described by equation (1), may be used or any other distance metric. These steps may be repeated if there are more than one pattern to be tested. The complete algorithm for pulsar selection is shown in Algorithm 1 listing.

---

#### Algorithm 1: Fuzzy knn Pulsar Selection Algorithm

---

**Input:** Test patterns matrix  $T$ , A candidate pulsar  $x$ ,  $k$

**Output:** A decision for  $x$  which is pulsar or not

**Steps:**

1. Construct the correlation matrix discovering features relationship
  2. Find the distance between  $x$  and  $T$  by Euclidean distance
  3. Select (pick) the first  $k$  samples (shortest distances)
  4. calculate the membership values to the  $k$  samples (soft labels) using equation 2.
  5. calculate the membership value to the two classes using equation 3
  6. Set the final class label = max
  7. Repeat steps 2-6 if there are more than one test pattern
  8. Use many folds to efficiently evaluate the classifier
- 

The main advantage of using fuzzy  $knn$  classifier is that, it doesn't assign a hard crisp membership that is used in the original  $knn$ . The "fuzzification" process ensures voting from different samples belonging to more than one classes, using the membership function, that may be considered as a weighted voting. The algorithm performs better if the  $k$  folds cross validation is used [13]. The  $k$ -fold cross validation is a technique used for better evaluation of classification algorithms. In this algorithm, the initial data are randomly partitioned into  $k$  mutually exclusive subsets, called folds,  $D_1, D_2, \dots, D_k$ . Each fold is approximately of equal size. The training and testing processes are performed  $k$  times. In iteration  $i$ , a partition  $D_i$  is reserved as the test set, and the remaining partitions are used together for training [13].

### 5. Experimental results

In this section, we will illustrate the classification results and evaluations of the proposed algorithm. In our experiments, we use MS Excel 2007 for figures drawing and some

computations. The Matlab R2012a is used for fuzzy *knn* implementation and results evaluation.

Firstly, we define some evaluation metrics that will be used in the comparison. The true positive (*TP*) is the number of candidate patterns that are already pulsars, and are also being classified as pulsars. The true negative (*TN*) is the number of candidates which are non-pulsars and also being classified as non pulsars. However, the false negative (*FN*) is the number of actual pulsar candidates that are incorrectly being classified as non pulsars. The false positive (*FP*) is the number of non-pulsars candidates that are incorrectly being classified as pulsars. The equations from 4 to 10 gives some important additional metrics that are computed for comparisons. More information about these metrics could be found in Refs. [1,9]. In general, good classifier should maximize the accuracy, precision, recall, F-score, specificity, and G-mean. However, the false positive rate (FPR) should be minimized.

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN} \quad (4)$$

$$FPR = \frac{FP}{FP + TN} \quad (5)$$

$$Precision = \frac{TP}{TP + FP} \quad (6)$$

$$Recall = \frac{TP}{TP + FN} \quad (7)$$

$$Fscore = 2 \times \frac{precision \times recall}{precision + recall} \quad (8)$$

$$Specificity = \frac{TN}{FP + TN} \quad (9)$$

$$GMean = \sqrt{\left(\frac{TP}{TP + FN} \times \frac{TN}{TN + FP}\right)} \quad (10)$$

In our experiments, all these metrics are computed to evaluate the performance of the proposed algorithm. Table 1 shows the correlation matrix [13] between the features  $X_i$  together, and between the features and the response variable  $Y$  (the output). It is clear that, most of the correlation values are normal.

However, there are four exceptions which are bolded. The first exception is between the input features  $X_3$  and  $X_4$  in which the correlation value equals 0.95 which is a strong correlation. Suggesting that, removing one feature of them may enhance the classification accuracy as the two features depend on each other. The second exception is between the features  $X_7$  and  $X_8$  which is also a strong positive correlation equals 0.92. The third exception is between the input variable  $X_7$  and the response variable  $Y$  which equals  $-0.39$ . This is a weak correlation between the input and the output suggesting that, removing  $X_7$  from the classification process may enhance the classification process. The final exception is between the input variable  $X_8$  and the output variable  $Y$  which is also a

Table 1  
The correlation matrix between features and output.

	$X_1$	$X_2$	$X_3$	$X_4$	$X_5$	$X_6$	$X_7$	$X_8$
$X_1$								
$X_2$	0.55							
$X_3$	-0.87	-0.52						
$X_4$	-0.74	-0.54	<b>0.95</b>					
$X_5$	-0.30	0.01	0.41	0.41				
$X_6$	-0.31	-0.05	0.43	0.42	0.80			
$X_7$	0.23	0.03	-0.34	-0.33	-0.62	-0.81		
$X_8$	0.14	0.03	-0.21	-0.20	-0.35	-0.58	<b>0.92</b>	
$Y$	-0.67	-0.36	0.79	0.71	0.40	0.49	<b>-0.39</b>	<b>-0.26</b>

Bold indicates maximum values and minimum values.

weak correlation equals  $-0.26$ , suggesting that, removing the variable  $X_8$  may enhances the classification accuracy. From these results, we make our experiments considering three cases; the first case is to use all input variables together in the classification. The second experiment is to remove both variables  $X_3, X_8$  and perform the classification. The final case is to remove only the variable  $X_8$  and consider all other variables in the classification. All these cases are shown next.

Regarding the work presented in Ref. [1], the authors evaluate the pulsar selection problem using five different classifiers; C4.5, MLP, NB, SVM, and their proposed GH-VFDT classifiers. The authors claim that, their proposed GH-VFDT classifier outperforms the other four classifiers. However, we will show here that, our proposed classifier outperforms all these five classifiers in many other evaluation metrics.

Fig. 1 shows the evaluation comparison of the six classifiers (the five classifiers compared in Ref. [1], and our proposed algorithm). The comparison here regarding the accuracy of the classifiers computed using equation (4). Here, we consider all eight input variables (features). It is clear from the figure that, the proposed algorithm outperforms the other five classifiers compared in Ref. [1]. However, although our proposed algorithm outperforms the other five classifiers, the accuracy difference between our algorithm and the GH-VFDT classifier is not very large. Comparing to the other four classifiers, our proposed algorithm has a significant performance increase compared to these algorithms.

The G-Mean computed from equation (10) is very important in pulsar selection problem [1]. Fig. 2 shows the

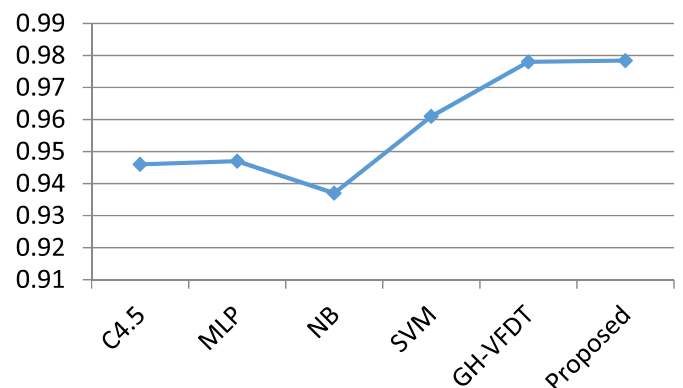


Fig. 1. Accuracy comparison.



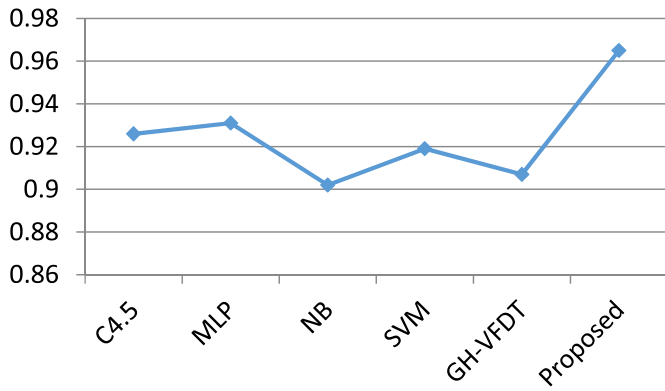


Fig. 2. G-mean comparison.

performance comparison of the G-mean of the six classifiers. The figure shows a significant increase in the G-mean of the proposed algorithm compared to the other five algorithms. It outperforms the MLP classifier by about 0.02, and outperforms the other classifiers by much more values.

Fig. 3 shows the performance comparison of the F-score shown by equation (8). The importance of F-score is that, it combines both the recall and the precision in one equation. Again, it is clear from Fig. 3 that, the proposed algorithm outperforms the other five algorithms in the F-score value.

Fig. 4 shows the performance comparison of the false positive rate (FPR) compared to the other five classifiers.

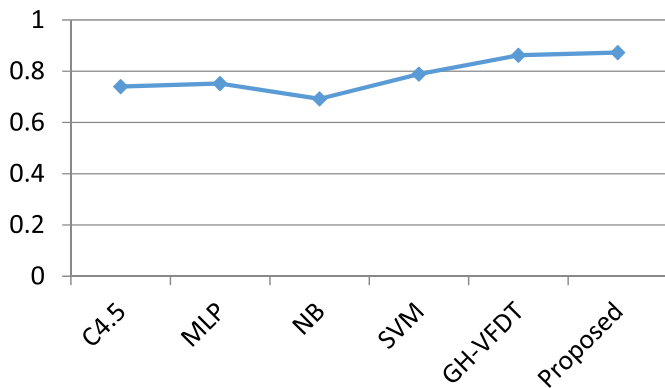


Fig. 3. F-score comparison.

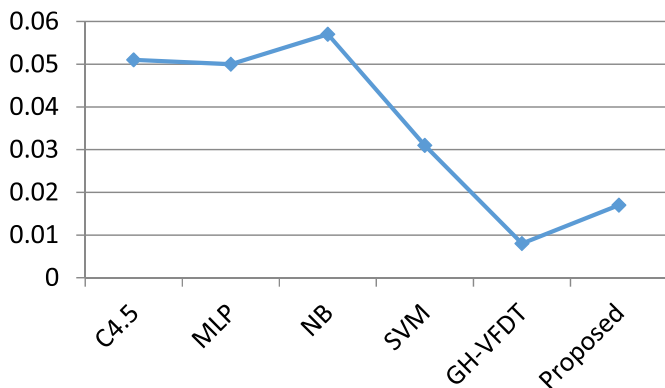


Fig. 4. FPR comparison.

Although, the proposed algorithm does not give the minimum FPR, however, it performs as the second ranked algorithm among the six classifiers. The first rated algorithm here is the GH-VFDT classifier proposed by Ref. [1]. In general, the FPR is required to be decreased to avoid extra telescope time for re-inspection of candidates by telescopes.

Table 2 shows more on the performance of the proposed algorithm using different features. There are three columns, the first column is the results obtained by using all input features. The second column gives the results obtained by excluding the variable  $X_8$  from classification. The third column gives the results obtained by excluding both variables  $X_3$  and  $X_8$ . Excluding of these variables is based on the correlation matrix obtained from Table 1 It is clear from the table that, using all features and excluding the variable  $X_8$  only are comparable in performance. Suggesting that, excluding of  $X_8$  leads to simplify the calculations as the number of features included in the computation are decreased. Moreover, both F-score and G-mean are enhanced by excluding the feature  $X_8$ . However, by excluding both features ( $X_3, X_8$ ), the performance is slightly decreased compared to the other two cases. This conclusion is very important, as opposite to the work in Ref. [1], which claim that, all features are important in the classification process.

Table 3 shows the effect of using different  $k$  values, in the cross validation process. The proposed algorithm is evaluated using different  $k$  values; 3, 5, 12, and 20. In all experiments, the constant  $m$ , described in equation (3), equals 0.3. It is clear that, there is no significant changes, of the performance metrics, between the different values of  $k$ . Suggesting that, the proposed algorithm is robust using the different values of  $k$ . However, the best performance parameters are obtained using values of  $k$  equals 5 and 12.

## 6. Conclusions

Pulsars are rare type of stars that emit radio signals detected from the earth. The process of pulsar selection is very complicated, and impractical to be performed manually. The neural network techniques are not always appropriate as there

Table 2  
Features effects.

	All	Excl. 8	Excl. 3, 8
Accuracy	0.978	0.978	0.972
f score	0.873	0.875	0.834
G-mean	0.961	0.962	0.954
FPR	0.17	0.17	0.23

Table 3  
Effects of k fold cross validation using all features.

	K = 3	K = 5	K = 12	K = 20
Accuracy	0.977	0.978	0.978	0.977
f score	0.866	0.873	0.870	0.870
G-mean	0.965	0.961	0.965	0.953
FPR	0.020	0.018	0.019	0.017

are some fuzziness in the features of the candidates. In this paper, we present a novel fuzzy *knn* technique to be used in pulsar selection process.

Results show that, the proposed algorithm outperforms five other classifiers in both accuracy, F-score, G-mean, and also in some other metrics. Results also show that, the features are not equally important. Further research is required to address the importance and relationship between the input features. The proposed algorithm is applied to the HTRU 2 dataset which is the latest dataset in pulsar selection domain.

## References

- [1] Lyon RJ, Stappers BW, Cooper S, Brooke JM, Knowles JD. Fifty years of pulsar candidate selection: from simple filters to a new principled real-time classification approach. *Mon Not R Astron Soc* June 2016;459(1): 1104–23.
- [2] Morello V, Barr ED, Bailes M, Flynn CM, Keane EF, van Straten W. SPINN: a straightforward machine learning solution to the pulsar candidate selection problem. *Mon Not R Astron Soc* 2014;443(2): 1651–62.
- [3] Lee KJ, Stovall K, Jenet FA, Martinez J, Dartez LP, Mata A, et al. PEACE: pulsar evaluation algorithm for candidate extraction—a software package for post-analysis processing of pulsar survey candidates. *Mon Not R Astron Soc* 2013;433(1):688–94.
- [4] Eatough RP, Molkenthin N, Kramer M, Noutsos A, Keith MJ, Stappers BW, et al. Selection of radio pulsar candidates using artificial neural networks. *Mon Not R Astron Soc* 2010;407(4):2443–50.
- [5] Thornton D. The high time resolution radio sky. PhD thesis. University of Manchester; 2013.
- [6] Bates SD, Bailes M, Barsdell BR, Bhat NDR, Burgay M, Burke-Spolaor S, et al. The high time resolution universe pulsar survey—VI. An artificial neural network and timing of 75 pulsars. *Mon Not R Astron Soc* 2012;427(2):1052–65.
- [7] Lorimer DR, Kramer M. *Handbook of pulsar astronomy*. Cambridge University Press; 2005.
- [8] The HTRU2 data set, last visited Nov. 13, 2017 <https://archive.ics.uci.edu/ml/datasets/HTRU2>.
- [9] Powers D. Evaluation: from precision, recall and F-measure to roc, informedness, markedness & correlation. *J Mach Learn Technol* 2011; 2(1):37–63.
- [10] Derrac J, Chiclana F, García S, Herrera F. Evolutionary fuzzy k-nearest neighbors algorithm using interval-valued fuzzy sets. *Inf Sci J* Feb. 2016; 329:144–63. ELSEVIER.
- [11] Keller JM, Gray MR, Givens JA. A fuzzy k-nearest neighbor algorithm. *IEEE Trans Syst Man Cybern* 1985;15(4):580–5.
- [12] Derrac J, García S, Herrera F. Fuzzy nearest neighbor algorithms: taxonomy, experimental analysis and prospects. *Inf Sci J* 2014;260:98–119.
- [13] Han J, Pei J, Kamber M. *Data mining: concepts and techniques*. 3rd ed. Elsevier; 2011.